

# The Possibilities are Infinite – Part 2

By





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## A MESSAGE FROM THE MATHEMATICS DIVISION OF THE MINISTRY OF EDUCATION

Skills such as logical thinking, higher-order thinking, and problem-solving play a significant role in the 21st century. Mathematics education is an effective tool for developing and embedding such skills. This book displays many instances that show the ability to enrich the reader with these skills. Apart from that, the book provides an opportunity for the reader to experience the beauty of mathematics and motivates them to enjoy the subject.

This book is designed with the base of contextual teaching and learning. It makes the readers aware of the mathematical history of the concepts, how the concepts are built up and discovered. This motivates the readers as it arouses their curiosity. This makes the book readable. The book has many challenging questions, and it gives logical argumentation as well. This helps the readers to develop their mathematical thinking.

It is a pleasure to see such books being written and presented to mathematics lovers. I wish all the best to the author of the book and hope for more and more creations in the future.

## Ms. P. P. Niroshi

Director of Mathematics Mathematics Division Ministry of Education Isurupaya.

09th of January 2025

## FOREWORD

It is with great admiration that I professionally endorse **BRAINSTORMER**, a mathematics resource book that benefits a broad audience including school students, teachers and academic researchers through its comprehensive and step-by-step approach to mathematics education.

In the 21st-century, the context of interdisciplinary learning enables students to achieve high-profile educational outcomes by promoting critical thinking. This book emphasizes the creation of mathematical models and formulation of computer programs to solve complex problems. The book follows a unique methodology starting with fundamental concepts including drawing figures and provides step-by-step guidance to ultimately reaching to a greater understanding of mathematics.

A testament to the author's innovative thinking is the publication of 17 new sequences on the Online Encyclopedia of Integer Sequences (OEIS), reflecting groundbreaking contributions to mathematics. These sequences not only enhance the field but also inspire students to think creatively and develop critical thinking and problem-solving skills.

The book further features seven articles on novel approaches to various mathematical topics. These articles are invaluable for understanding contemporary developments in mathematics. The quality of this author's contributions has been internationally recognized as evident by his invitation as a referee for the prominent academic journal, the College Mathematics Journal of the Mathematical Association of America.

Additionally, **BRAINSTORMER** introduces the Humanistic Mathematics Activity-Based Project, a pioneering initiative that effectively generates student interest in mathematics and motivates them to pursue higher academic goals. The criteria for selecting activities and the examples provided in the book offer excellent guidance for teachers to design their own activity sessions.

While it is practically impossible to deliver mathematics education to perfection due to resource limitations and the constraints of exam-oriented Syllabi, **BRAINSTORMER** provides practical guidance to learn mathematics in an interactive and meaningful way. This is not merely a vision, but a reality demonstrated through the exemplary commitments of its Founder Chairman.

I highly recommend **BRAINSTORMER** for its innovative contributions to mathematics education and its ability to inspire learners, educators, and researchers alike. It is a significant asset to the mathematics field and a commendable effort toward elevating the standards of mathematics education.

## Dr. (Mrs.) Kissani Perera

Senior lecturer and a Former Head of the Department of Mathematics University of Kelaniya Sri Lanka January 26, 2025

## PREFACE

Most of us are born lateral thinkers, naturally inclined to use nontraditional and unconventional approaches to problem-solving. This type of thinking is crucial for developing creativity and exploratory skills. However, many lose their lateral thinking abilities in schools and universities due to the adoption of vertical thinking, which emphasizes strict adherence to rules and focusing on a single answer. This approach limits our brains to a fixed frame, giving very little opportunity to enhance exploratory skills in mathematics.

In my first prime document **"The Possibilities are Infinite"**, I have provided numerous examples where lateral thinking is essential to transforming the reader into an explorer. Preparing students' mindsets before they enter secondary education is crucial for them to fully benefit from this document. Therefore, I prepared the second prime document, "**Maths Projects for Grades 8, 9, 10, and Ordinary Level Students**," which introduces maths activities for students up to the ordinary level standard.

This third document **BRAINSTORMER** consists of a **new concept** of combinatorial geometry, **17 new** sequences in mathematics published on the OEIS, and 7 new proofs. Among these is a fully trigonometric proof of Pythagoras' theorem that does not rely on the properties of similar triangles, and the first-ever single proof of both the Sine Law and the Cosine Law. Related articles not only introduce novel approaches but also guide readers in formatting manuscripts to international standards. Additionally, it includes a pioneering initiative Humanistic Mathematics Activity-Based Project and establishing the Brainstormer Foundation for the development of mathematics education. This document aims to provide significant evidence that supports my vision articulated in the first document. The positive feedback from senior lecturers at leading universities, who reviewed the first document, further validates this vision. As a result, users can be confident in the value of the information provided in the first document, which aim to transform the current system of mathematics education into a more contextual teaching and learning process. This transformation holds the promise of producing mathematicians who can appreciate the importance of mathematical issues, view the world through the lens of mathematics, describe both physical activities and the wonders of nature in mathematical terms, tackle global challenges, and create their own challenges and conjectures that extend beyond conventional human understanding. I believe that the provided mathematical models and computer programs will be helpful for the students who are doing ICT as a subject and academics in their research within the software field, ultimately fulfilling the goals of  $21^{st}$  century mathematics education.

I extend my sincere gratitude to the board of editors of the **Online Encyclopedia of Integer Sequences** for recognizing the importance of new concepts and assisting in drafting my submissions to international standards. My heartfelt thanks go to the editors of the **Mathematical Association of America** journals for reviewing my submissions and providing valuable feedback. Special thanks to **Rev. Bro. Director Dr. Pubudu Rajapaksha** for his support in initiating the Humanistic Mathematics Activity-Based Project at the college, and to **Dr. (Mrs.) Kissani Perera** for graciously providing the **FOREWORD** for the **BRAINSTORMER**.

## Janaka Rodrigo

Founder Chairman BRAINSTORMER FOUNDATION Sri Lanka January 27, 2025

# **CONTRIBUTIONS TO MATHEMATICS**

## New concept in Combinatorial Geometry (Pages 1 to 3)

1) Partitioning the set of vertices of a convex polygon into nonintersecting polygons.

## Sequences published on Online Encyclopedia of Integer Sequences (OEIS) ( Pages 4 to 22 )

- 2) A350116 Number of ways to partition the set of vertices of a convex (n +8) gon into 3 nonintersecting polygons.
- 3) A350248 Triangle read by rows T(n,k) is the number of non-crossing partitions of an n set into k blocks of size 3 or more, n > = 0, 0 < = k < = floor (n/3)
- 4) A350286 Number of different ways to partition the set of vertices of a convex (n + 11) gon into 4 nonintersecting polygons.
- 5) A350303 Number of ways to partition the set of vertices of a convex (n + 14) gon into 5 nonintersecting polygons.
- 6) A350599 Number of ways to partition the set of vertices of a convex n gon into nonintersecting directed polygons.
- 7) A350640 Minimum lcm of the part sizes of a partition of n into parts of size 3 or more.
- A347862 Total number of polygons left out in all partitions of the set of vertices of a convex n – gon into nonintersecting polygons.
- 9) A351103 Total number of polygons left over with maximum number of sides when partitioning the set of vertices of a convex n gon into nonintersecting polygons.
- 10) A352477 Number of different ways to partition the set of vertices of a convex n gon into 4 intersecting polygons.
- 11) A352474 Number of different ways to partition the set of vertices of a convex n gon into 3 intersecting polygons.
- 12) A352611 Number of different ways to partition the set of vertices of a convex n gon into 5 polygons.
- 13) A352900 Number of different ways to partition the set of vertices of a convex n gon into intersecting polygons.
- 14) A357603 Number of different pairs of shortest paths in an n X n lattice going between opposite corners in opposite direction and not meeting at their middle point.
- 15) A357760 Number of different pairs of shortest grid paths joining two opposite corners in opposite order in an n X n X n grid with middle point on the paths as a common point.
- 16) A358481 Number of different pairs of shortest grid paths joining two opposite corners in opposite order in an n X n X n grid without having middle point on their paths as a common point.
- 17) A362207 Number of unordered triples of shortest nonintersecting grid paths joining two opposite corners of an n X n X n grid.
- 18) A360444 Number of ways for two nonintersecting, unordered pairs of shortest grid paths to cross over between two opposite corners in an n X n grid without intersecting opposite paths at their middle points.

## Mathematical Models and Computer Programs in Combinatorial Geometry (Pages 23 to 28)

- 19) Mathematical Model of the sequence A360444.
- 20) Python Code of the Mathematical Model of A360444
- 21) Mathematical Model of ordered triplets (An open challenge to create a computer program and obtain integer outputs)

# New proofs and totally different approaches in other fields of mathematics (Pages 29 to 44)

- 22) Geometrical proof of the sum of infinite series  $\cot^{-1} 3 + \cot^{-1} 7 + \cot^{-1} 13 + \dots$  converges to  $\pi/4$ .
- 23) Geometrical proof of the sum of infinite series  $\cot^{-1} 2 + \cot^{-1} 8 + \cot^{-1} 18 + \dots$  converges to  $\pi/4$ .
- 24) Geometrical proof of the sum of infinite series  $\frac{1}{1.2} + \frac{1}{2.3} + \frac{1}{3.4} + \dots$  converges to 1.
- 25) Geometrical proof of sum and the product of three tangents of a triangle are equal in the case of an obtuse-angled triangles.
- 26) The Inclusion-Exclusion Principle in geometrical approach of completing square in Quadratics.
- 27) Fully trigonometric proof of Pythagoras theorem without applying properties of similar triangles.
- 28) Simultaneous Single Proof of the Sine Law and Cosine Law.

## 21<sup>st</sup> Century Teaching and Learning Mathematics (Pages 45 to 56)

- 29) Humanistic Mathematics Activity-Based Project.
- 30) Brainstormer Foundation

#### ANNEXURE

31) Geometric Abstract Art Lesson Plan